



# Bits, Bytes and Integers – Part 1

15-213/18-213/15-513: Introduction to Computer Systems  
2<sup>nd</sup> Lecture, Aug. 31, 2017

**Today's Instructor:**

Randy Bryant

# Announcements

- Recitations are on Mondays, but next Monday (9/4) is Labor Day, so recitations are cancelled
- Linux Boot Camp Monday evening 7pm, Rashid Auditorium
- Lab 0 is now available via course web page and [Autolab](#).
  - Due Thu Sept. 7, 11:59pm
  - No grace days
  - No late submissions
  - Just do it!

# Waitlist questions

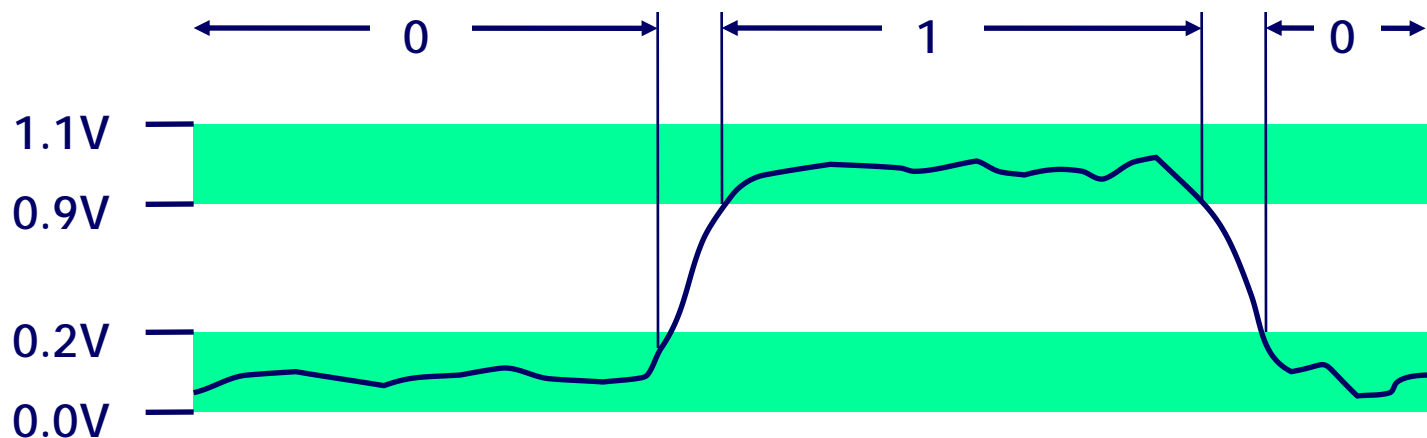
- 15-213: Mary Widom ([marwidom@cs.cmu.edu](mailto:marwidom@cs.cmu.edu))
- 18-213: ECE Academic services  
[ece-asc@andrew.cmu.edu](mailto:ece-asc@andrew.cmu.edu)
- 15-513: Mary Widom ([marwidom@cs.cmu.edu](mailto:marwidom@cs.cmu.edu))
- Please don't contact the instructors with waitlist questions.

# Today: Bits, Bytes, and Integers

- **Representing information as bits**
- **Bit-level manipulations**
- **Integers**
  - Representation: unsigned and signed
  - Conversion, casting
  - Expanding, truncating
  - Addition, negation, multiplication, shifting
  - Summary
- **Representations in memory, pointers, strings**

# Everything is bits

- Each bit is 0 or 1
- By encoding/interpreting sets of bits in various ways
  - Computers determine what to do (instructions)
  - ... and represent and manipulate numbers, sets, strings, etc...
- Why bits? Electronic Implementation
  - Easy to store with bistable elements
  - Reliably transmitted on noisy and inaccurate wires



# For example, can count in binary

## ■ Base 2 Number Representation

- Represent  $15213_{10}$  as  $11101101101101_2$
- Represent  $1.20_{10}$  as  $1.0011001100110011[0011]..._2$
- Represent  $1.5213 \times 10^4$  as  $1.1101101101101_2 \times 2^{13}$

# Encoding Byte Values

## ■ Byte = 8 bits

- Binary  $00000000_2$  to  $11111111_2$
- Decimal:  $0_{10}$  to  $255_{10}$
- Hexadecimal  $00_{16}$  to  $FF_{16}$ 
  - Base 16 number representation
  - Use characters '0' to '9' and 'A' to 'F'
  - Write  $FA1D37B_{16}$  in C as
    - `0xFA1D37B`
    - `0xfa1d37b`

| Hex | Decimal | Binary |
|-----|---------|--------|
| 0   | 0       | 0000   |
| 1   | 1       | 0001   |
| 2   | 2       | 0010   |
| 3   | 3       | 0011   |
| 4   | 4       | 0100   |
| 5   | 5       | 0101   |
| 6   | 6       | 0110   |
| 7   | 7       | 0111   |
| 8   | 8       | 1000   |
| 9   | 9       | 1001   |
| A   | 10      | 1010   |
| B   | 11      | 1011   |
| C   | 12      | 1100   |
| D   | 13      | 1101   |
| E   | 14      | 1110   |
| F   | 15      | 1111   |

15213:    0011   1011   0110   1101  
                  3            B            6            D



# Example Data Representations

| C Data Type          | Typical 32-bit | Typical 64-bit | x86-64 |
|----------------------|----------------|----------------|--------|
| <code>char</code>    | 1              | 1              | 1      |
| <code>short</code>   | 2              | 2              | 2      |
| <code>int</code>     | 4              | 4              | 4      |
| <code>long</code>    | 4              | 8              | 8      |
| <code>float</code>   | 4              | 4              | 4      |
| <code>double</code>  | 8              | 8              | 8      |
| <code>pointer</code> | 4              | 8              | 8      |

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# Boolean Algebra

## ■ Developed by George Boole in 19th Century

- Algebraic representation of logic
  - Encode “True” as 1 and “False” as 0

And

- $A \& B = 1$  when both  $A=1$  and  $B=1$

| $\&$ | 0 | 1 |
|------|---|---|
| 0    | 0 | 0 |
| 1    | 0 | 1 |

Or

- $A | B = 1$  when either  $A=1$  or  $B=1$

| $ $ | 0 | 1 |
|-----|---|---|
| 0   | 0 | 1 |
| 1   | 1 | 1 |

Not

- $\sim A = 1$  when  $A=0$

| $\sim$ |   |
|--------|---|
| 0      | 1 |
| 1      | 0 |

Exclusive-Or (Xor)

- $A \wedge B = 1$  when either  $A=1$  or  $B=1$ , but not both

| $\wedge$ | 0 | 1 |
|----------|---|---|
| 0        | 0 | 1 |
| 1        | 1 | 0 |

# General Boolean Algebras

## ■ Operate on Bit Vectors

- Operations applied bitwise

|                   |                   |                   |                   |
|-------------------|-------------------|-------------------|-------------------|
| 01101001          | 01101001          | 01101001          |                   |
| & 01010101        | 01010101          | ^ 01010101        | ~ 01010101        |
| <u>          </u> | <u>          </u> | <u>          </u> | <u>          </u> |
| 01000001          | 01111101          | 00111100          | 10101010          |

## ■ All of the Properties of Boolean Algebra Apply

# Example: Representing & Manipulating Sets

## ■ Representation

- Width  $w$  bit vector represents subsets of  $\{0, \dots, w-1\}$
- $a_j = 1$  if  $j \in A$

- 01101001       $\{0, 3, 5, 6\}$

- 76543210

- 01010101       $\{0, 2, 4, 6\}$

- 76543210

## ■ Operations

- |                             |          |                        |
|-----------------------------|----------|------------------------|
| ▪ &    Intersection         | 01000001 | $\{0, 6\}$             |
| ▪      Union                | 01111101 | $\{0, 2, 3, 4, 5, 6\}$ |
| ▪ ^    Symmetric difference | 00111100 | $\{2, 3, 4, 5\}$       |
| ▪ ~    Complement           | 10101010 | $\{1, 3, 5, 7\}$       |

# Bit-Level Operations in C

## ■ Operations $\&$ , $|$ , $\sim$ , $\wedge$ Available in C

- Apply to any “integral” data type
  - *long, int, short, char, unsigned*
- View arguments as bit vectors
- Arguments applied bit-wise

## ■ Examples (Char data type)

- $\sim 0x41 \rightarrow$
- $\sim 0x00 \rightarrow$
- $0x69 \& 0x55 \rightarrow$
- $0x69 | 0x55 \rightarrow$

| Hex | Decimal | Binary |
|-----|---------|--------|
| 0   | 0       | 0000   |
| 1   | 1       | 0001   |
| 2   | 2       | 0010   |
| 3   | 3       | 0011   |
| 4   | 4       | 0100   |
| 5   | 5       | 0101   |
| 6   | 6       | 0110   |
| 7   | 7       | 0111   |
| 8   | 8       | 1000   |
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| D   | 13      | 1101   |
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| F   | 15      | 1111   |

# Bit-Level Operations in C

## ■ Operations $\&$ , $|$ , $\sim$ , $\wedge$ Available in C

- Apply to any “integral” data type
  - *long, int, short, char, unsigned*
- View arguments as bit vectors
- Arguments applied bit-wise

## ■ Examples (Char data type)

- $\sim 0x41 \rightarrow 0xBE$ 
  - $\sim 0100\ 0001_2 \rightarrow 1011\ 1110_2$
- $\sim 0x00 \rightarrow 0xFF$ 
  - $\sim 0000\ 0000_2 \rightarrow 1111\ 1111_2$
- $0x69 \& 0x55 \rightarrow 0x41$ 
  - $0110\ 1001_2 \& 0101\ 0101_2 \rightarrow 0100\ 0001_2$
- $0x69 | 0x55 \rightarrow 0x7D$ 
  - $0110\ 1001_2 | 0101\ 0101_2 \rightarrow 0111\ 1101_2$

| Hex | Decimal | Binary |
|-----|---------|--------|
| 0   | 0       | 0000   |
| 1   | 1       | 0001   |
| 2   | 2       | 0010   |
| 3   | 3       | 0011   |
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# Contrast: Logic Operations in C

## ■ Contrast to Bit-Level Operators

### ■ Logic Operations: `&`, `||`, `!`

- View 0 as “False”

- Anything nonzero

- Always

- Early

## ■ Example

- `!0x41` →

- `!0x00` →

- `!!0x41` → `0x01`

- `0x69 && 0x55` → `0x01`

- `0x69 || 0x55` → `0x01`

- `p && *p` (avoids null pointer access)

Watch out for `&&` vs. `&` (and `||` vs. `|`)...  
one of the more common oopsies in  
C programming



# Shift Operations

## ■ Left Shift: $x \ll y$

- Shift bit-vector  $x$  left  $y$  positions
  - Throw away extra bits on left
  - Fill with 0's on right

## ■ Right Shift: $x \gg y$

- Shift bit-vector  $x$  right  $y$  positions
  - Throw away extra bits on right
- Logical shift
  - Fill with 0's on left
- Arithmetic shift
  - Replicate most significant bit on left

## ■ Undefined Behavior

- Shift amount  $< 0$  or  $\geq$  word size

|                |          |
|----------------|----------|
| Argument $x$   | 01100010 |
| $\ll 3$        | 00010000 |
| Log. $\gg 2$   | 00011000 |
| Arith. $\gg 2$ | 00011000 |

|                |          |
|----------------|----------|
| Argument $x$   | 10100010 |
| $\ll 3$        | 00010000 |
| Log. $\gg 2$   | 00101000 |
| Arith. $\gg 2$ | 11101000 |

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# Encoding Integers

## Unsigned

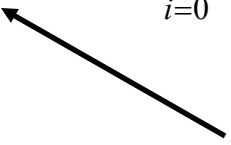
$$B2U(X) = \sum_{i=0}^{w-1} x_i \cdot 2^i$$

## Two's Complement

$$B2T(X) = -x_{w-1} \cdot 2^{w-1} + \sum_{i=0}^{w-2} x_i \cdot 2^i$$

```
short int x = 15213;
short int y = -15213;
```

Sign Bit



## ■ C short 2 bytes long

|          | Decimal | Hex   | Binary            |
|----------|---------|-------|-------------------|
| <b>x</b> | 15213   | 3B 6D | 00111011 01101101 |
| <b>y</b> | -15213  | C4 93 | 11000100 10010011 |

## ■ Sign Bit

- For 2's complement, most significant bit indicates sign
  - 0 for nonnegative
  - 1 for negative

# Two-complement: Simple Example

$$\begin{array}{rcccccc}
 & & -16 & 8 & 4 & 2 & 1 \\
 10 = & 0 & 1 & 0 & 1 & 0 & 
 \end{array}
 \qquad
 8+2 = 10$$

$$\begin{array}{rcccccc}
 & & -16 & 8 & 4 & 2 & 1 \\
 -10 = & 1 & 0 & 1 & 1 & 0 & 
 \end{array}
 \qquad
 -16+4+2 = -10$$

# Two-complement Encoding Example (Cont.)

$x =$             15213: 00111011 01101101  
 $y =$             -15213: 11000100 10010011

| Weight     | 15213        |      | -15213        |        |
|------------|--------------|------|---------------|--------|
| 1          | 1            | 1    | 1             | 1      |
| 2          | 0            | 0    | 1             | 2      |
| 4          | 1            | 4    | 0             | 0      |
| 8          | 1            | 8    | 0             | 0      |
| 16         | 0            | 0    | 1             | 16     |
| 32         | 1            | 32   | 0             | 0      |
| 64         | 1            | 64   | 0             | 0      |
| 128        | 0            | 0    | 1             | 128    |
| 256        | 1            | 256  | 0             | 0      |
| 512        | 1            | 512  | 0             | 0      |
| 1024       | 0            | 0    | 1             | 1024   |
| 2048       | 1            | 2048 | 0             | 0      |
| 4096       | 1            | 4096 | 0             | 0      |
| 8192       | 1            | 8192 | 0             | 0      |
| 16384      | 0            | 0    | 1             | 16384  |
| -32768     | 0            | 0    | 1             | -32768 |
| <b>Sum</b> | <b>15213</b> |      | <b>-15213</b> |        |

# Numeric Ranges

## ■ Unsigned Values

- $UMin = 0$   
000...0
- $UMax = 2^w - 1$   
111...1

## ■ Two's Complement Values

- $TMin = -2^{w-1}$   
100...0
- $TMax = 2^{w-1} - 1$   
011...1
- Minus 1  
111...1

### Values for $W = 16$

|             | Decimal       | Hex          | Binary                   |
|-------------|---------------|--------------|--------------------------|
| <b>UMax</b> | <b>65535</b>  | <b>FF FF</b> | <b>11111111 11111111</b> |
| <b>TMax</b> | <b>32767</b>  | <b>7F FF</b> | <b>01111111 11111111</b> |
| <b>TMin</b> | <b>-32768</b> | <b>80 00</b> | <b>10000000 00000000</b> |
| <b>-1</b>   | <b>-1</b>     | <b>FF FF</b> | <b>11111111 11111111</b> |
| <b>0</b>    | <b>0</b>      | <b>00 00</b> | <b>00000000 00000000</b> |

# Values for Different Word Sizes

|      | W    |         |                |                            |
|------|------|---------|----------------|----------------------------|
|      | 8    | 16      | 32             | 64                         |
| UMax | 255  | 65,535  | 4,294,967,295  | 18,446,744,073,709,551,615 |
| TMax | 127  | 32,767  | 2,147,483,647  | 9,223,372,036,854,775,807  |
| TMin | -128 | -32,768 | -2,147,483,648 | -9,223,372,036,854,775,808 |

## ■ Observations

- $|TMin| = TMax + 1$ 
  - Asymmetric range
- $UMax = 2 * TMax + 1$

## ■ C Programming

- `#include <limits.h>`
- Declares constants, e.g.,
  - `ULONG_MAX`
  - `LONG_MAX`
  - `LONG_MIN`
- Values platform specific

# Unsigned & Signed Numeric Values

| $X$  | $B2U(X)$ | $B2T(X)$ |
|------|----------|----------|
| 0000 | 0        | 0        |
| 0001 | 1        | 1        |
| 0010 | 2        | 2        |
| 0011 | 3        | 3        |
| 0100 | 4        | 4        |
| 0101 | 5        | 5        |
| 0110 | 6        | 6        |
| 0111 | 7        | 7        |
| 1000 | 8        | -8       |
| 1001 | 9        | -7       |
| 1010 | 10       | -6       |
| 1011 | 11       | -5       |
| 1100 | 12       | -4       |
| 1101 | 13       | -3       |
| 1110 | 14       | -2       |
| 1111 | 15       | -1       |

## ■ Equivalence

- Same encodings for nonnegative values

## ■ Uniqueness

- Every bit pattern represents unique integer value
- Each representable integer has unique bit encoding

## ■ $\Rightarrow$ Can Invert Mappings

- $U2B(x) = B2U^{-1}(x)$ 
  - Bit pattern for unsigned integer
- $T2B(x) = B2T^{-1}(x)$ 
  - Bit pattern for two's comp integer



# Quiz Time!

Check out:

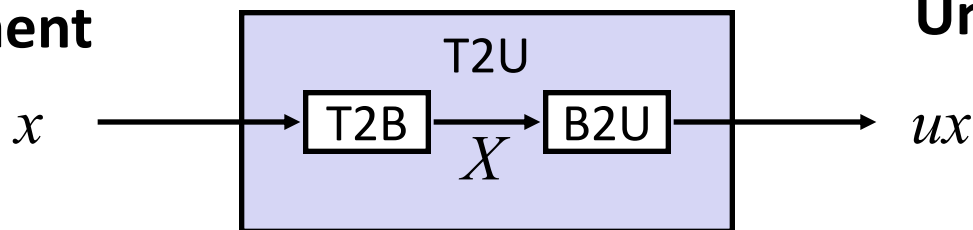
<https://canvas.cmu.edu/courses/1221>

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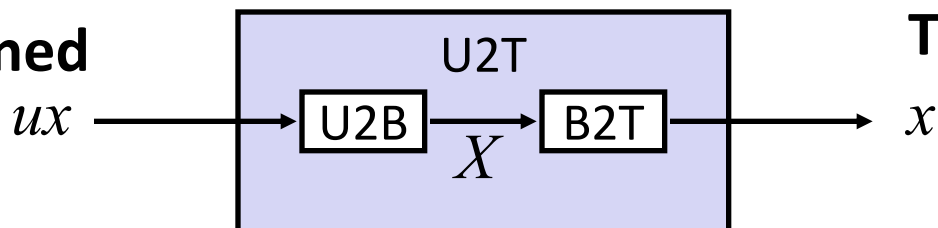
# Mapping Between Signed & Unsigned

Two's Complement



Maintain Same Bit Pattern

Unsigned



Maintain Same Bit Pattern

- Mappings between unsigned and two's complement numbers:  
**Keep bit representations and reinterpret**

# Mapping Signed $\leftrightarrow$ Unsigned

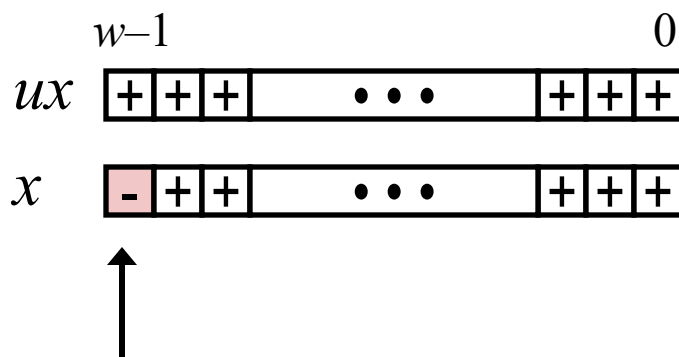
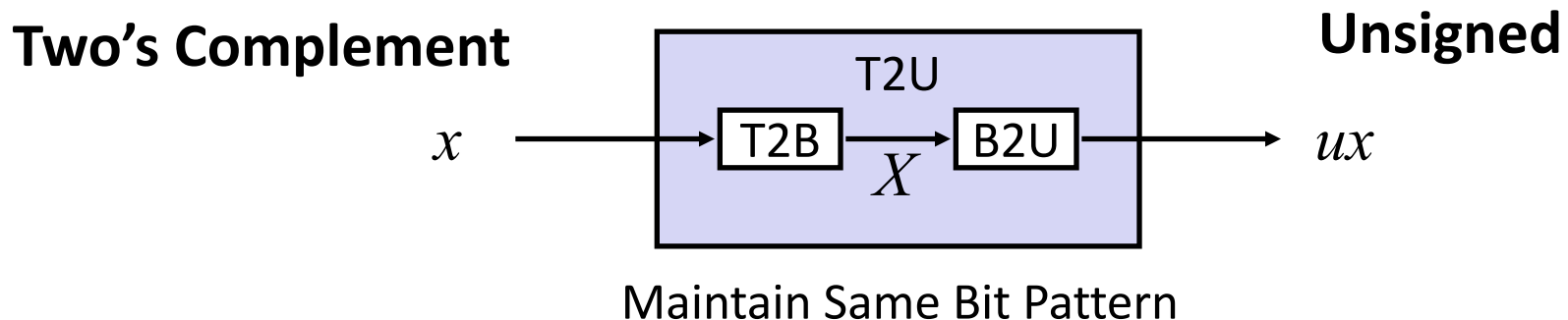
| Bits | Signed |  | Unsigned |
|------|--------|--|----------|
| 0000 | 0      |  | 0        |
| 0001 | 1      |  | 1        |
| 0010 | 2      |  | 2        |
| 0011 | 3      |  | 3        |
| 0100 | 4      |  | 4        |
| 0101 | 5      |  | 5        |
| 0110 | 6      |  | 6        |
| 0111 | 7      |  | 7        |
| 1000 | -8     |  | 8        |
| 1001 | -7     |  | 9        |
| 1010 | -6     |  | 10       |
| 1011 | -5     |  | 11       |
| 1100 | -4     |  | 12       |
| 1101 | -3     |  | 13       |
| 1110 | -2     |  | 14       |
| 1111 | -1     |  | 15       |

$\rightarrow$  **T2U**  $\rightarrow$   
 $\leftarrow$  **U2T**  $\leftarrow$

# Mapping Signed $\leftrightarrow$ Unsigned

| Bits | Signed |                                 | Unsigned |
|------|--------|---------------------------------|----------|
| 0000 | 0      | $\longleftrightarrow$<br>=      | 0        |
| 0001 | 1      |                                 | 1        |
| 0010 | 2      |                                 | 2        |
| 0011 | 3      |                                 | 3        |
| 0100 | 4      |                                 | 4        |
| 0101 | 5      |                                 | 5        |
| 0110 | 6      |                                 | 6        |
| 0111 | 7      |                                 | 7        |
| 1000 | -8     | $\longleftrightarrow$<br>+/- 16 | 8        |
| 1001 | -7     |                                 | 9        |
| 1010 | -6     |                                 | 10       |
| 1011 | -5     |                                 | 11       |
| 1100 | -4     |                                 | 12       |
| 1101 | -3     |                                 | 13       |
| 1110 | -2     |                                 | 14       |
| 1111 | -1     |                                 | 15       |

# Relation between Signed & Unsigned

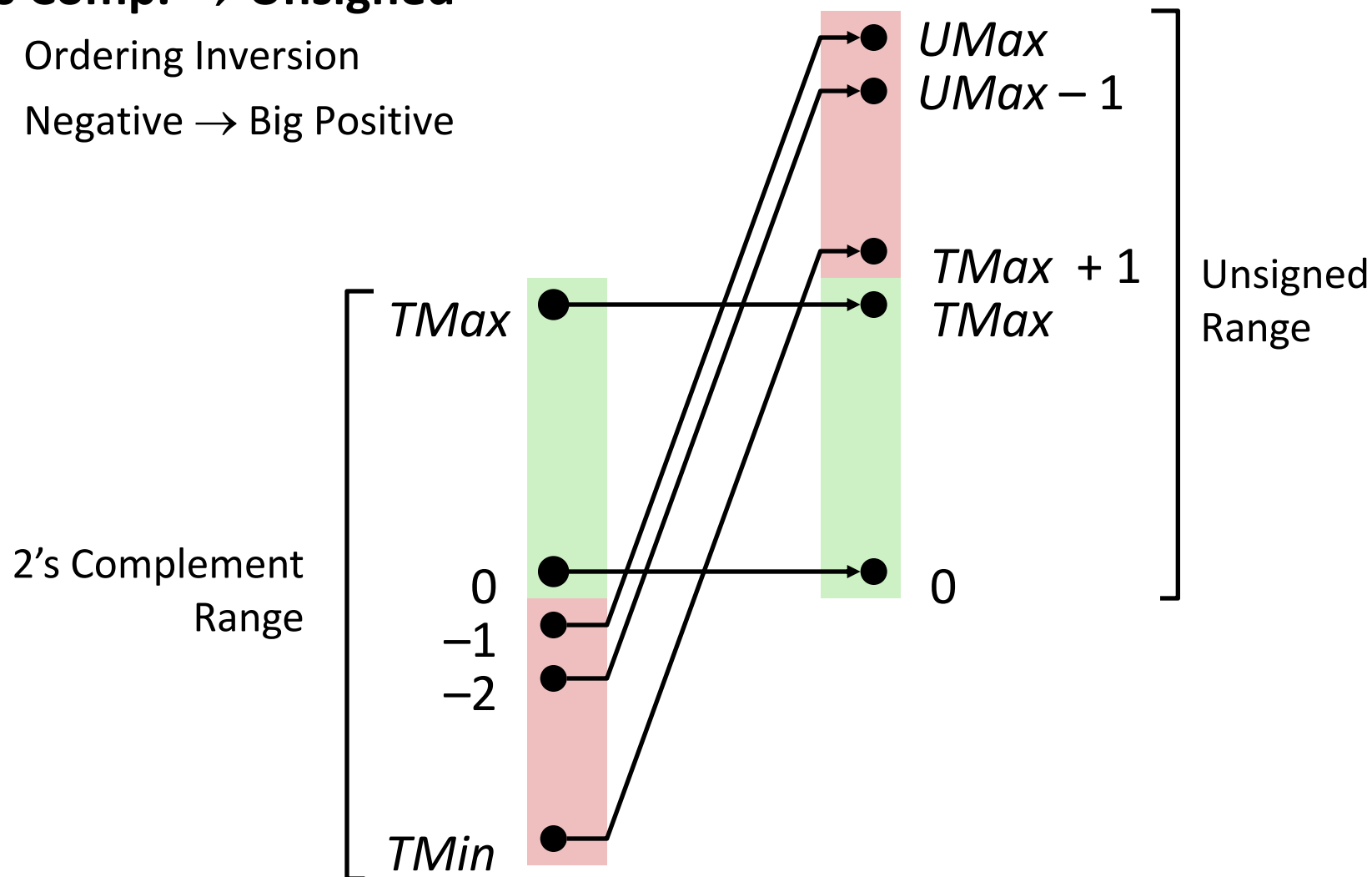


Large negative weight  
*becomes*  
 Large positive weight

# Conversion Visualized

## ■ 2's Comp. → Unsigned

- Ordering Inversion
- Negative → Big Positive



# Signed vs. Unsigned in C

## ■ Constants

- By default are considered to be signed integers
- Unsigned if have “U” as suffix

`0U, 4294967259U`

## ■ Casting

- Explicit casting between signed & unsigned same as U2T and T2U

```
int tx, ty;  
unsigned ux, uy;  
tx = (int) ux;  
uy = (unsigned) ty;
```

- Implicit casting also occurs via assignments and procedure calls

```
tx = ux;                                int fun(unsigned u);  
uy = ty;                                uy = fun(tx);
```



# Casting Surprises

## ■ Expression Evaluation

- If there is a mix of unsigned and signed in single expression,  
*signed values implicitly cast to unsigned*
- Including comparison operations  $<$ ,  $>$ ,  $==$ ,  $<=$ ,  $>=$
- Examples for  $W = 32$ : **TMIN = -2,147,483,648**, **TMAX = 2,147,483,647**

| ■ Constant <sub>1</sub> | Constant <sub>2</sub> | Relation | Evaluation |
|-------------------------|-----------------------|----------|------------|
| 0                       | 0U                    | ==       | unsigned   |
| -1                      | 0                     | <        | signed     |
| -1                      | 0U                    | >        | unsigned   |
| 2147483647              | -2147483647-1         | >        | signed     |
| 2147483647U             | -2147483647-1         | <        | unsigned   |
| -1                      | -2                    | >        | signed     |
| (unsigned)-1            | -2                    | >        | unsigned   |
| 2147483647              | 2147483648U           | <        | unsigned   |
| 2147483647              | (int) 2147483648U     | >        | signed     |

# Unsigned vs. Signed: Easy to Make Mistakes

```
unsigned i;  
for (i = cnt-2; i >= 0; i--)  
    a[i] += a[i+1];
```

- Can be very subtle

```
#define DELTA sizeof(int)  
int i;  
for (i = CNT; i-DELTA >= 0; i-= DELTA)  
    . . .
```

# Summary

## Casting Signed $\leftrightarrow$ Unsigned: Basic Rules

- Bit pattern is maintained
- But reinterpreted
- Can have unexpected effects: adding or subtracting  $2^w$
- Expression containing signed and unsigned int
  - `int` is cast to `unsigned`!!

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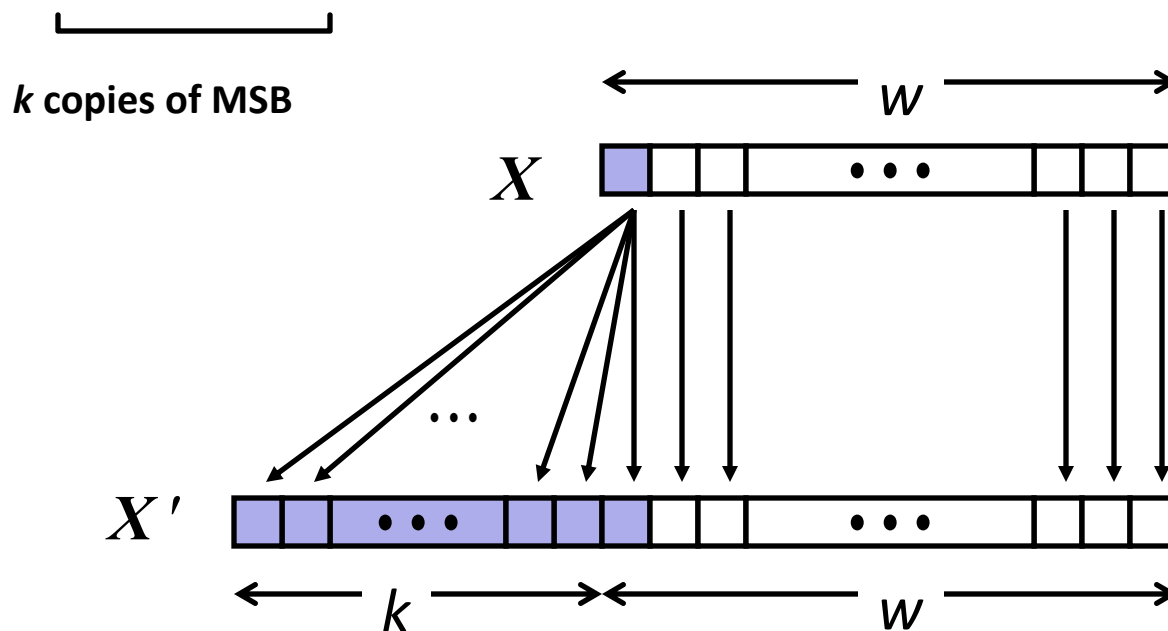
# Sign Extension

## ■ Task:

- Given  $w$ -bit signed integer  $x$
- Convert it to  $w+k$ -bit integer with same value

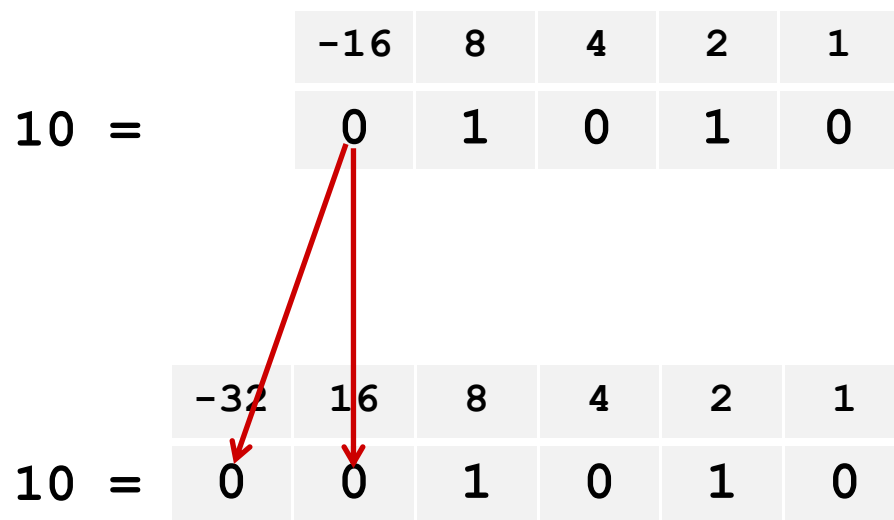
## ■ Rule:

- Make  $k$  copies of sign bit:
- $X' = \underbrace{x_{w-1}, \dots, x_{w-1}}_{k \text{ copies of MSB}}, x_{w-1}, x_{w-2}, \dots, x_0$

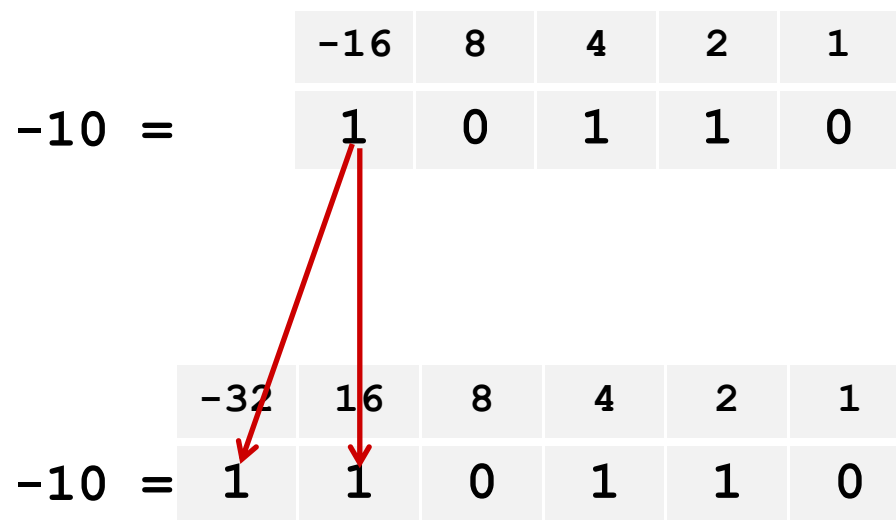


# Sign Extension: Simple Example

## Positive number



## Negative number



# Larger Sign Extension Example

```
short int x = 15213;
int      ix = (int) x;
short int y = -15213;
int      iy = (int) y;
```

|           | Decimal | Hex         | Binary                              |
|-----------|---------|-------------|-------------------------------------|
| <b>x</b>  | 15213   | 3B 6D       | 00111011 01101101                   |
| <b>ix</b> | 15213   | 00 00 3B 6D | 00000000 00000000 00111011 01101101 |
| <b>y</b>  | -15213  | C4 93       | 11000100 10010011                   |
| <b>iy</b> | -15213  | FF FF C4 93 | 11111111 11111111 11000100 10010011 |

- Converting from smaller to larger integer data type
- C automatically performs sign extension

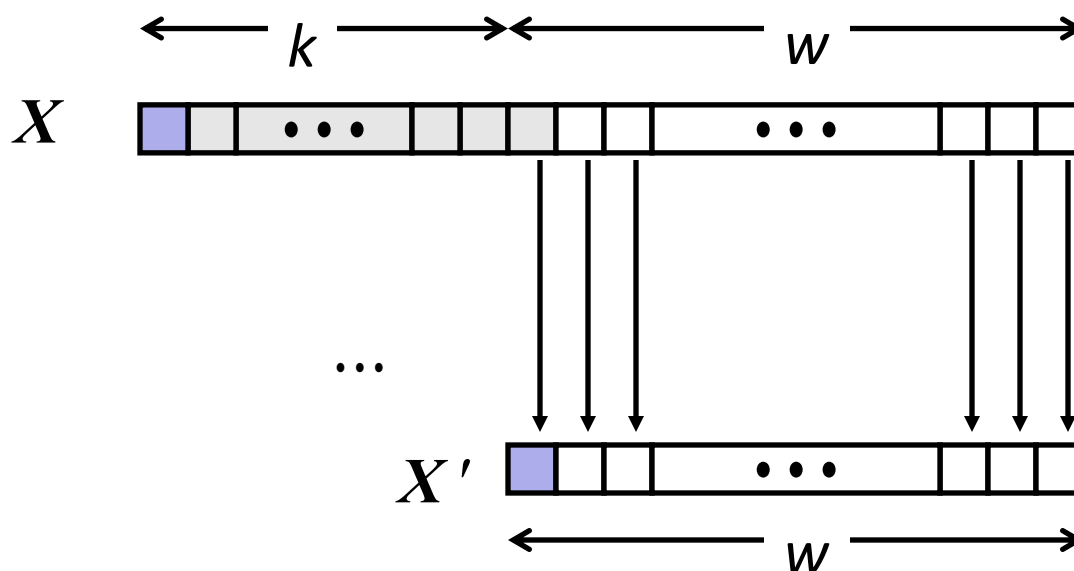
# Truncation

## ■ Task:

- Given  $k+w$ -bit signed or unsigned integer  $X$
- Convert it to  $w$ -bit integer  $X'$  with same value for “small enough”  $X$

## ■ Rule:

- Drop top  $k$  bits:
- $X' = x_{w-1}, x_{w-2}, \dots, x_0$





# Truncation: Simple Example

## No sign change

|     |     |   |   |   |   |
|-----|-----|---|---|---|---|
|     | -16 | 8 | 4 | 2 | 1 |
| 2 = | 0   | 0 | 0 | 1 | 0 |

|     |    |   |   |   |
|-----|----|---|---|---|
|     | -8 | 4 | 2 | 1 |
| 2 = | 0  | 0 | 1 | 0 |

$$2 \bmod 16 = 2$$

|      |     |   |   |   |   |
|------|-----|---|---|---|---|
|      | -16 | 8 | 4 | 2 | 1 |
| -6 = | 1   | 1 | 0 | 1 | 0 |

|      |    |   |   |   |
|------|----|---|---|---|
|      | -8 | 4 | 2 | 1 |
| -6 = | 1  | 0 | 1 | 0 |

$$-6 \bmod 16 = 26 \text{U} \bmod 16 = 10 \text{U} = -6$$

## Sign change

|      |     |   |   |   |   |
|------|-----|---|---|---|---|
|      | -16 | 8 | 4 | 2 | 1 |
| 10 = | 0   | 1 | 0 | 1 | 0 |

|      |    |   |   |   |
|------|----|---|---|---|
|      | -8 | 4 | 2 | 1 |
| -6 = | 1  | 0 | 1 | 0 |

$$10 \bmod 16 = 10 \text{U} \bmod 16 = 10 \text{U} = -6$$

|       |     |   |   |   |   |
|-------|-----|---|---|---|---|
|       | -16 | 8 | 4 | 2 | 1 |
| -10 = | 1   | 0 | 1 | 1 | 0 |

|     |    |   |   |   |
|-----|----|---|---|---|
|     | -8 | 4 | 2 | 1 |
| 6 = | 0  | 1 | 1 | 0 |

$$-10 \bmod 16 = 22 \text{U} \bmod 16 = 6 \text{U} = 6$$

# Summary:

## Expanding, Truncating: Basic Rules

- **Expanding (e.g., short int to int)**
  - Unsigned: zeros added
  - Signed: sign extension
  - Both yield expected result
  
- **Truncating (e.g., unsigned to unsigned short)**
  - Unsigned/signed: bits are truncated
  - Result reinterpreted
  - Unsigned: mod operation
  - Signed: similar to mod
  - For small (in magnitude) numbers yields expected behavior

# Summary of Today: Bits, Bytes, and Integers

- Representing information as bits
- Bit-level manipulations
- Integers
  - Representation: unsigned and signed
  - Conversion, casting
  - Expanding, truncating
  - Addition, negation, multiplication, shifting
- Representations in memory, pointers, strings
- Summary